

# Package ‘nhppp’

May 29, 2024

**Title** Simulating Nonhomogeneous Poisson Point Processes

**Version** 0.1.4

**Description** Simulates events from one dimensional nonhomogeneous Poisson point processes (NH-PPPs) as per Trikalinos and Sereda (2024, <[doi:10.48550/arXiv.2402.00358](https://doi.org/10.48550/arXiv.2402.00358)>). Functions are based on three algorithms that provably sample from a target NHPPP: the time-transformation of a homogeneous Poisson process (of intensity one) via the inverse of the integrated intensity function (Cinlar E, "Theory of stochastic processes" (1975, ISBN:0486497996)); the generation of a Poisson number of order statistics from a fixed density function; and the thinning of a majorizing NHPPP via an acceptance-rejection scheme (Lewis PAW, Shedler, GS (1979) <[doi:10.1002/nav.3800260304](https://doi.org/10.1002/nav.3800260304)>).

**License** GPL (>= 3)

**Imports** lifecycle, rstream, Rcpp (>= 1.0.12)

**LinkingTo** Rcpp

**Encoding** UTF-8

**Language** es

**RoxygenNote** 7.3.1

**Suggests** data.table, rlecuyer, testthat, withr

**Config/Needs/website** rmarkdown

**URL** <https://github.com/bladder-ca/nhppp>

**BugReports** <https://github.com/bladder-ca/nhppp/issues>

**NeedsCompilation** yes

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**Repository** CRAN

**Date/Publication** 2024-05-28 22:50:02 UTC

**R topics documented:**

check_ppp_sample_validity . . . . .	3
check_ppp_vector_validity . . . . .	4
compare_ppp_vectors . . . . .	4
draw . . . . .	5
draw_cumulative_intensity_inversion . . . . .	6
draw_cumulative_intensity_orderstats . . . . .	7
draw_intensity . . . . .	8
draw_intensity_step . . . . .	9
draw_sc_linear . . . . .	10
draw_sc_loglinear . . . . .	11
draw_sc_step . . . . .	12
draw_sc_step_regular . . . . .	13
expect_no_error . . . . .	14
get_step_majorizer . . . . .	14
inverse_with_uniroot . . . . .	15
inverse_with_uniroot_sorted . . . . .	16
Lambda_exp_form . . . . .	17
Lambda_inv_exp_form . . . . .	17
Lambda_inv_linear_form . . . . .	18
Lambda_linear_form . . . . .	18
make_cumulative_Lambda_matrix . . . . .	19
make_lambda_matrix . . . . .	19
make_range_t_matrix . . . . .	20
mat_cumsum_columns . . . . .	20
mat_cumsum_columns_with_scalar_ceiling . . . . .	21
mat_cumsum_columns_with_vector_ceiling . . . . .	21
mat_diff_columns . . . . .	22
ppp_n . . . . .	22
ppp_next_n . . . . .	23
ppp_orderstat . . . . .	24
ppp_sequential . . . . .	24
read_code . . . . .	25
rng_stream_rexp . . . . .	26
rng_stream_rpois . . . . .	26
rng_stream_runif . . . . .	27
rng_stream_rztpois . . . . .	27
rztpois . . . . .	28
simpson_num_integr . . . . .	28
vdraw . . . . .	29
vdraw_intensity_step_regular . . . . .	30
vdraw_intensity_step_regular_cpp . . . . .	31
vdraw_intensity_step_regular_R . . . . .	32
vdraw_sc_step_regular . . . . .	34
vdraw_sc_step_regular_cpp . . . . .	35
vdraw_sc_step_regular_R . . . . .	36
vztdraw_intensity_step_regular . . . . .	37

*check\_ppp\_sample\_validity* 3

<i>vzdraw_intensity_step_regular_R</i> . . . . .	38
<i>vzdraw_sc_step_regular</i> . . . . .	39
<i>vzdraw_sc_step_regular_cpp</i> . . . . .	40
<i>vzdraw_sc_step_regular_R</i> . . . . .	41
<i>ztdraw_cumulative_intensity</i> . . . . .	42
<i>ztdraw_intensity</i> . . . . .	43
<i>ztdraw_intensity_step</i> . . . . .	44
<i>ztdraw_sc_linear</i> . . . . .	45
<i>ztdraw_sc_loglinear</i> . . . . .	46
<i>ztppp</i> . . . . .	47

**Index** 48

---

*check\_ppp\_sample\_validity*  
*Check the validity of ppp samples*

---

### Description

Standard checks for a vector of ordered times. Check that the `times` vector is sorted, has unique values, has all values in `[t_min, t_max]`, and has length `size` (if applicable).

### Usage

```
check_ppp_sample_validity(  
  times,  
  t_min,  
  t_max = NULL,  
  size = NULL,  
  atmost1 = FALSE,  
  atleast1 = FALSE  
)
```

### Arguments

<code>times</code>	(vector, double   matrix) the times to be checked as vectors or matrices (time-vectors in rows)
<code>t_min</code>	(double) the start of the time interval
<code>t_max</code>	(double) optional: the end of the time interval
<code>size</code>	(double) optional: the size of the vector
<code>atmost1</code>	(boolean) optional: at most one sample returned
<code>atleast1</code>	(boolean) optional: at least one sample returned

### Value

None

---

check\_ppp\_vector\_validity

*Check the validity of a ppp vector.*

---

### Description

Standard checks for a vector of ordered times. Check that the times vector is sorted, has unique values, has all values in [t\_min, t\_max], and has length size (if applicable).

### Usage

```
check_ppp_vector_validity(
  times,
  t_min,
  t_max = NULL,
  size = NULL,
  atmost1 = FALSE,
  atleast1 = FALSE
)
```

### Arguments

times	(vector, double) the times to be checked
t_min	(double) the start of the time interval
t_max	(double) optional: the end of the time interval
size	(double) optional: the size of the vector
atmost1	(boolean) optional: at most one sample returned
atleast1	(boolean) optional: at least one sample returned

### Value

None

---

compare\_ppp\_vectors *Check that two ppp vectors Q-Q agree*

---

### Description

Compare that the deciles of two vectors have absolute difference over average ratios less than threshold

### Usage

```
compare_ppp_vectors(ppp1, ppp2, threshold = 0.15, showQQ = TRUE)
```

**Arguments**

ppp1	(vector, double) the first vector
ppp2	(vector, double) the second vector
threshold	(double) optional: the cutoff for a large absolute threshold
showQQ	(boolean) optional: show the QQ plot if the absolute value of the Difference vs Average ratio in any decile is bigger than the threshold

**Value**

None

---

draw	<i>Generic function for simulating from NHPPs given the intensity function or the cumulative intensity function.</i>
------	--

---

**Description**

This is a wrapper to the package's specific functions, and thus somewhat slower. For time-intensive simulations prefer one of the specific functions.

**Usage**

```
draw(
  lambda = NULL,
  lambda_maj = NULL,
  Lambda = NULL,
  Lambda_inv = NULL,
  range_t = c(0, 10),
  rng_stream = NULL,
  atmost1 = FALSE,
  atleast1 = FALSE
)
```

**Arguments**

lambda	(function) the instantaneous rate of the NHPP. A continuous function of time.
lambda_maj	(double, vector) the intercept and optional slope of the majorizing linear (if exp_maj = FALSE) or log-linear (if exp_maj = TRUE) function in range_t.
Lambda	(function, double vector) a continuous increasing R to R map which is the integrated rate of the NHPP
Lambda_inv	(function, double vector) the inverse of Lambda()
range_t	(vector, double) min and max of the time interval.
rng_stream	(rstream) an rstream object or NULL
atmost1	boolean, draw at most 1 event time
atleast1	boolean, draw at least 1 event time in interval

**Value**

a vector of event times

---

draw\_cumulative\_intensity\_inversion

*Simulate from a non homogeneous Poisson Point Process (NHPPP)  
from (t\_min, t\_max) (inversion method)*

---

**Description**

Sample NHPPP times using the inversion method, optionally using an rstream generator object

**Usage**

```
draw_cumulative_intensity_inversion(
  Lambda,
  Lambda_inv = NULL,
  range_t = c(0, 10),
  range_L = c(Lambda(range_t[1]), Lambda(range_t[2])),
  rng_stream = NULL,
  atmost1 = FALSE
)
```

**Arguments**

Lambda	(function, double vector) a continuous increasing R to R map which is the integrated rate of the NHPPP
Lambda_inv	(function, double vector) the inverse of Lambda()
range_t	(vector, double) min and max of the time interval
range_L	(vector, double) min and max of the transformed time interval
rng_stream	(rstream) an rstream object.
atmost1	boolean, draw at most 1 event time

**Value**

a vector of event times (t\_); if no events realize, a vector of length 0

**Examples**

```
x <- draw_cumulative_intensity_inversion(Lambda = function(t) t + cos(t) - 1)
```

---

`draw_cumulative_intensity_orderstats`

*Simulate from a non homogeneous Poisson Point Process (NHPPP)  
from (t\_min, t\_max) (order statistics method)*

---

## Description

Sample NHPPP times using the order statistics method, optionally using an rstream generator object.

## Usage

```
draw_cumulative_intensity_orderstats(  
  Lambda,  
  Lambda_inv = NULL,  
  range_t = c(0, 10),  
  range_L = c(Lambda(range_t[1]), Lambda(range_t[2])),  
  rng_stream = NULL,  
  atmost1 = FALSE  
)
```

## Arguments

<code>Lambda</code>	(function, double vector) a continuous increasing R to R map which is the integrated rate of the NHPPP
<code>Lambda_inv</code>	(function, double vector) the inverse of <code>Lambda()</code>
<code>range_t</code>	(vector, double) min and max of the time interval
<code>range_L</code>	(vector, double) min and max of the transformed time interval
<code>rng_stream</code>	(rstream) an rstream object or NULL.
<code>atmost1</code>	boolean, draw at most 1 event time

## Value

a vector of event times (`t_`); if no events realize, a vector of length 0

## Examples

```
x <- draw_cumulative_intensity_orderstats(Lambda = function(t) t + cos(t) - 1)
```

---

draw_intensity	<i>Simulate from a non homogeneous Poisson Point Process (NHPPP) from (t0, t_max) (thinning method)</i>
----------------	---

---

### Description

Sample NHPPP times using the thinning method, optionally using an rstream generator

### Usage

```
draw_intensity(
  lambda,
  lambda_maj = NULL,
  exp_maj = FALSE,
  range_t = c(0, 10),
  rng_stream = NULL,
  atmost1 = FALSE
)
```

### Arguments

lambda	(function) the instantaneous rate of the NHPPP. A continuous function of time.
lambda_maj	(double, vector) the intercept and optional slope of the majorizing linear (if exp_maj = FALSE) or log-linear (if exp_maj = TRUE) function in range_t.
exp_maj	(boolean) if TRUE the majorizer is $\exp(\alpha + \beta * t)$
range_t	(vector, double) min and max of the time interval.
rng_stream	(rstream) an rstream object or NULL
atmost1	boolean, draw at most 1 event time

### Value

a vector of event times (t\_); if no events realize, a vector of length 0

### Examples

```
x <- draw_intensity(lambda = function(t) 1 + sin(t))
```

---

draw_intensity_step	<i>Simulate from a non homogeneous Poisson Point Process (NHPPP) from (t0, t_max) (thinning method) with piecewise constant_majorizer</i>
---------------------	---

---

## Description

Sample NHPPP times using the thinning method, optionally using an rstream generator

## Usage

```
draw_intensity_step(
  lambda,
  lambda_maj_vector = lambda(1:10),
  times_vector = 0:10,
  rng_stream = NULL,
  atmost1 = FALSE
)
```

## Arguments

lambda	(function) the instantaneous rate of the NHPPP. A continuous function of time.
lambda_maj_vector	(scalar, double) K constant majorizing rates, one per interval
times_vector	(vector, double) K+1 time points defining K intervals of constant rates: [t_1 = range_t[1], t_2): the first interval [t_k, t_{k+1}): the k-th interval [t_{K}, t_{K+1} = range_t[2]): the K-th (last) interval
rng_stream	(rstream) an rstream object or NULL
atmost1	boolean, draw at most 1 event time

## Value

a vector of event times (t\_); if no events realize, a vector of length 0

## Examples

```
x <- draw_intensity_step(lambda = function(t) exp(.02 * t))
```

---

draw_sc_linear	<i>Special case: Simulate from a non homogeneous Poisson Point Process (NHPPP) from (t_min, t_max) with linear intensity function (inversion method)</i>
----------------	--

---

### Description

Sample NHPPP times from a linear intensity function using the inversion method, optionally using an rstream generator

### Usage

```
draw_sc_linear(
  alpha = 1,
  beta = 0,
  range_t = c(0, 10),
  rng_stream = NULL,
  atmost1 = FALSE
)
```

### Arguments

alpha	(double) the intercept
beta	(double) the slope
range_t	(vector, double) min and max of the time interval
rng_stream	(rstream) an rstream object.
atmost1	boolean, draw at most 1 event time

### Value

a vector of event times (t\_); if no events realize, a vector of length 0

### Examples

```
x <- draw_sc_linear(alpha = 0, beta = 0.2)
```

---

draw_sc_loglinear	<i>Special case: Simulate from a non homogeneous Poisson Point Process (NHPPP) from <math>(t_{min}, t_{max})</math> with log-linear intensity function (inversion method)</i>
-------------------	---

---

## Description

Sample NHPPP times from an log linear intensity function using the inversion method, optionally using an `rstream` generator

## Usage

```
draw_sc_loglinear(  
  alpha = 1,  
  beta = 0,  
  range_t = c(0, 10),  
  rng_stream = NULL,  
  atmost1 = FALSE  
)
```

## Arguments

<code>alpha</code>	(double) the intercept in the exponent
<code>beta</code>	(double) the slope in the exponent
<code>range_t</code>	(vector, double) min and max of the time interval
<code>rng_stream</code>	( <code>rstream</code> ) an <code>rstream</code> object.
<code>atmost1</code>	boolean, draw at most 1 event time

## Value

a vector of event times (`t_`); if no events realize, a vector of length 0

## Examples

```
x <- draw_sc_loglinear(alpha = 0, beta = 0.2)
```

---

draw_sc_step	<i>Simulate a piecewise constant-rate Poisson Point Process over (t_min, t_max] (inversion method) The intervals need not have the same length.</i>
--------------	---

---

### Description

Simulate a piecewise constant-rate Poisson Point Process over (t\_min, t\_max] (inversion method)  
The intervals need not have the same length.

### Usage

```
draw_sc_step(
  lambda_vector = rep(1, 5),
  times_vector = c(0:5),
  rng_stream = NULL,
  atmost1 = FALSE,
  atleast1 = FALSE
)
```

### Arguments

lambda_vector	(scalar, double) K constant rates, one per interval
times_vector	(vector, double) K+1 time points defining K intervals of constant rates: [t_1 = range_t[1], t_2): the first interval [t_k, t_{k+1}): the k-th interval [t_{K}, t_{K+1} = range_t[2]): the K-th (last) interval
rng_stream	an rstream object
atmost1	boolean, draw at most 1 event time
atleast1	boolean, draw at least 1 event time

### Value

a vector of event times t if no events realize, it will have 0 length

### Examples

```
x <- draw_sc_step(lambda_vector = rep(1, 5), times_vector = c(0:5))
```

---

draw\_sc\_step\_regular    *Sampling from NHPPs with piecewise constant intensities with same interval lengths (non-vectorized)*

---

## Description

Sampling from NHPPs with piecewise constant intensities with same interval lengths (non-vectorized)

## Usage

```
draw_sc_step_regular(  
  Lambda_vector = NULL,  
  lambda_vector = NULL,  
  range_t = c(0, 10),  
  rng_stream = NULL,  
  atmost1 = FALSE,  
  atleast1 = FALSE  
)
```

## Arguments

`Lambda_vector` (scalar, double) K integrated intensity rates at the end of each interval

`lambda_vector` (scalar, double) K constant intensity rates, one per interval

`range_t` (vector, double) `t_min` and `t_max`

`rng_stream` an `rstream` object

`atmost1` boolean, draw at most 1 event time

`atleast1` boolean, draw at least 1 event time

## Value

a vector of event times `t` if no events realize, it will have 0 length

## Examples

```
x <- draw_sc_step_regular(Lambda_vector = 1:5, range_t = c(0, 5))
```

---

expect_no_error	<i>Helper functions</i>
-----------------	-------------------------

---

**Description**

helper function that augments `test_that::expect_no_error()` to expect no error. Copied from the R6 source code.

**Usage**

```
expect_no_error(expr)
```

**Arguments**

expr	Expression.
------	-------------

**Details**

Small utility functions. Not to be exported to the user.

---

get_step_majorizer	<i>Piecewise constant (step) majorizer for K-Lipschitz functions over an interval (vectorized over the breaks argument).</i>
--------------------	--

---

**Description**

Return a piecewise constant (step) majorizer for K-Lipschitz functions over an interval. The function is vectorized over the breaks argument.

**Usage**

```
get_step_majorizer(fun, breaks, is_monotone = TRUE, K = 0)
```

**Arguments**

fun	A function object with a single argument <code>x</code> . If <code>x</code> is a matrix, <code>fun</code> should be vectorized over it.
breaks	(vector or matrix) The set of $M+1$ boundaries for the $M$ subintervals in <code>x</code> . If <code>breaks</code> is a matrix, each row is treated as a separate set of breaks.
is_monotone	(boolean) Is the function monotone? (Default is TRUE.)
K	(double) A non-negative number for the Lipschitz cone. (Default is 0.)

**Value**

A vector of length  $M$  with the values of the piecewise constant majorizer

**Examples**

```
get_step_majorizer(fun = abs, breaks = -5:5, is_monotone = FALSE, K = 1)
```

---

inverse\_with\_uniroot *Numerically evaluate the inverse of a function at a specific point*

---

**Description**

Numerically evaluate the inverse of a function at a specific point

**Usage**

```
inverse_with_uniroot(  
  f = f,  
  y,  
  min_x = 0,  
  max_x = 1,  
  min_y = f(min_x),  
  max_y = f(max_x)  
)
```

**Arguments**

f	(function) the function to be inverted; must be continuous and increasing
y	(scalar, double) the $f(x)=y$ value in which to evaluate the inverse
min_x	(scalar, double) the min of the domain of f()
max_x	(scalar, double) the max of the domain of f()
min_y	(scalar, double) the min in the range of f()
max_y	(scalar, double) the max in the range of f()

**Value**

(scalar, double) vector of  $x=f^{-1}(y)$ : the inverted value

**Examples**

```
inverse_with_uniroot(f = function(x) {  
  2 * x  
}, y = 0.5)
```

---

`inverse_with_uniroot_sorted`

*Numerically evaluate the inverse of a monotonically increasing continuous function from  $R$  to  $R$  at specific points.*

---

### Description

Numerically evaluate the inverse of a monotonically increasing continuous function from  $R$  to  $R$  at specific points.

### Usage

```
inverse_with_uniroot_sorted(  
  f,  
  y,  
  range_x = c(0, 10),  
  range_y = c(f(range_x[1]), f(range_x[2]))  
)
```

### Arguments

<code>f</code>	(function) the function to be inverted; must be continuous and increasing
<code>y</code>	(vector, double) the $f(x)=y$ values in which to evaluate the inverse; must be in ascending order
<code>range_x</code>	(vector, double) the min and max of the domain of $f()$
<code>range_y</code>	(vector, double) the min and max in the range of $f()$

### Value

(vector, double) vector of  $x=f^{-1}(y)$ : the inverted values

### Examples

```
inverse_with_uniroot_sorted(f = function(x) {  
  2 * x  
}, y = c(0, 0.5))
```

---

Lambda\_exp\_form      *Definite integral of  $l = \exp(\alpha + \beta \cdot t)$  at time  $t$  with  $L(t_0) = 0$*

---

**Description**

Definite integral of  $l = \exp(\alpha + \beta \cdot t)$  starting at  $t_0$  – only for  $l+$ .

**Usage**

Lambda\_exp\_form( $t$ ,  $\alpha$ ,  $\beta$ ,  $t_0$ )

**Arguments**

$t$                     (double) the time point  
 $\alpha$                  (double) the intercept  
 $\beta$                    (double) the slope  
 $t_0$                   (double) the starting time

---

Lambda\_inv\_exp\_form      *Inverse of the definite integral of  $l = \exp(\alpha + \beta \cdot t)$  at time  $t$*

---

**Description**

Inverse of the definite integral of  $l = \exp(\alpha + \beta \cdot t)$  only for  $l+$ .

**Usage**

Lambda\_inv\_exp\_form( $z$ ,  $\alpha$ ,  $\beta$ ,  $t_0$ )

**Arguments**

$z$                     (double) the value of integrated rate for which you want to find the time  
 $\alpha$                  (double) the intercept  
 $\beta$                    (double) the slope  
 $t_0$                   (double) the starting time

---

Lambda\_inv\_linear\_form

*Inverse of the definite integral of  $l = \alpha + \beta \cdot t$  at time  $t$*

---

### Description

Inverse of the definite integral of  $l = \alpha + \beta \cdot t$  only for  $l+$ .

### Usage

Lambda\_inv\_linear\_form(z, alpha, beta, t0)

### Arguments

z	(double) the value of integrated rate for which you want to find the time
alpha	(double) the intercept
beta	(double) the slope
t0	(double) the starting time

---

Lambda\_linear\_form     *Definite integral of  $l = \alpha + \beta \cdot t$  at time  $t$  with  $L(t_0) = 0$*

---

### Description

Definite integral of  $l = \alpha + \beta \cdot t$  starting at  $t_0$  – only for  $l+$ .

### Usage

Lambda\_linear\_form(t, alpha, beta, t0)

### Arguments

t	(double) the time point
alpha	(double) the intercept
beta	(double) the slope
t0	(double) the starting time

---

```
make_cumulative_Lambda_matrix
```

*Helper function for the vectorized versions of sampling functions. Takes the usual ways that lambda\_mat and Lambda\_mat are specified and returns Lambda\_mat.*

---

### Description

Helper function for the vectorized versions of sampling functions. Takes the usual ways that lambda\_mat and Lambda\_mat are specified and returns Lambda\_mat.

### Usage

```
make_cumulative_Lambda_matrix(  
  Lambda_mat = NULL,  
  lambda_mat = NULL,  
  interval_duration = NULL  
)
```

### Arguments

Lambda\_mat      a matrix of cumulative intensities or missing  
lambda\_mat      a matrix of intensities or missing  
interval\_duration      a vector with the same number of elements as the rows of Lambda\_mat

### Value

A matrix (r x 2), row-expanded if needed

---

```
make_lambda_matrix      Helper function for the vectorized versions of sampling functions. Takes the usual ways that lambda_mat and Lambda_mat are specified and returns lambda_mat.
```

---

### Description

Helper function for the vectorized versions of sampling functions. Takes the usual ways that lambda\_mat and Lambda\_mat are specified and returns lambda\_mat.

### Usage

```
make_lambda_matrix(  
  lambda_mat = NULL,  
  Lambda_mat = NULL,  
  interval_duration = NULL  
)
```

**Arguments**

lambda\_mat        a matrix of intensities or missing  
 Lambda\_mat        a matrix of cumulative intensities or missing  
 interval\_duration  
                     a vector with the same number of elements as the rows of Lambda\_mat

**Value**

A matrix (r x 2), row-expanded if needed

---

make\_range\_t\_matrix    *Helper function for the vectorized versions of sampling functions. Takes the usual ways that range\_t is specified (a 2-vector, a 1 x 2 or an r x 2 matrix) and returns a r x 2 matrix.*

---

**Description**

Helper function for the vectorized versions of sampling functions. Takes the usual ways that range\_t is specified (a 2-vector, a 1 x 2 or an r x 2 matrix) and returns a r x 2 matrix.

**Usage**

```
make_range_t_matrix(range_t, n_rows)
```

**Arguments**

range\_t            a 2-vector, a 1 x 2 or an r x 2 matrix  
 n\_rows            the number of rows in the fully expanded matrix (r)

**Value**

A matrix (r x 2), row-expanded if needed

---

mat\_cumsum\_columns    *Return matrix with column-wise cumulative sum No checks for arguments is done.*

---

**Description**

Return matrix with column-wise cumulative sum No checks for arguments is done.

**Usage**

```
mat_cumsum_columns(X)
```

**Arguments**

X (matrix)

**Value**

matrix

---

mat\_cumsum\_columns\_with\_scalar\_ceiling

*Return matrix with column-wise cumulative sum replacing cells larger than ceil with NA. No checks for arguments is done.*

---

**Description**

Return matrix with column-wise cumulative sum replacing cells larger than ceil with NA. No checks for arguments is done.

**Usage**

```
mat_cumsum_columns_with_scalar_ceiling(X, ceil = Inf)
```

**Arguments**

X (matrix)  
ceil (double or Inf) the ceiling to be applied

**Value**

matrix

---

mat\_cumsum\_columns\_with\_vector\_ceiling

*Return matrix with column-wise cumulative sum replacing cells larger than ceil with NA. No checks for arguments is done.*

---

**Description**

Return matrix with column-wise cumulative sum replacing cells larger than ceil with NA. No checks for arguments is done.

**Usage**

```
mat_cumsum_columns_with_vector_ceiling(X, ceil = Inf)
```

**Arguments**

`X` (matrix)  
`ceil` (vector or Inf) the set of ceilings to be applied, per row of `X`

**Value**

matrix

---

`mat_diff_columns` *Return matrix with column-wise differencing. No checks for arguments is done.*

---

**Description**

Return matrix with column-wise differencing. No checks for arguments is done.

**Usage**

`mat_diff_columns(X)`

**Arguments**

`X` (matrix)

**Value**

matrix

---

`ppp_n` *Simulate specific number of points from a homogeneous Poisson Point Process over  $(t_{min}, t_{max}]$*

---

**Description**

Simulate specific number of points from a homogeneous Poisson Point Process over  $(t_{min}, t_{max}]$

**Usage**

`ppp_n(size, range_t = c(0, 10), rng_stream = NULL)`

**Arguments**

`size` (int) the number of points to be simulated  
`range_t` (vector, double) min and max of the time interval  
`rng_stream` an `rstream` object

**Value**

a vector of event times of size size

**Examples**

```
x <- ppp_n(size = 10, range_t = c(0, 10))
```

---

ppp\_next\_n

*Simulate n events from a homogeneous Poisson Point Process.*

---

**Description**

Simulate n events from a homogeneous Poisson Point Process.

**Usage**

```
ppp_next_n(n = 1, rate = 1, t_min = 0, rng_stream = NULL)
```

**Arguments**

n	scalar number of samples
rate	scalar instantaneous rate
t_min	scalar for the starting time value
rng_stream	an rstream object

**Value**

a vector with event times t (starting from t\_min)

**Examples**

```
x <- ppp_next_n(n = 10, rate = 1, t_min = 0)
```

---

ppp_orderstat	<i>Simulate a homogeneous Poisson Point Process over (t_min, t_max] (order statistics method)</i>
---------------	---

---

**Description**

Simulate a homogeneous Poisson Point Process over (t\_min, t\_max] (order statistics method)

**Usage**

```
ppp_orderstat(range_t = c(0, 10), rate = 1, rng_stream = NULL, atmost1 = FALSE)
```

**Arguments**

range_t	(vector, double) min and max of the time interval
rate	(scalar, double) constant instantaneous rate
rng_stream	an rstream object
atmost1	boolean, draw at most 1 event time

**Value**

a vector of event times t if no events realize, it will have 0 length

**Examples**

```
x <- ppp_orderstat(range_t = c(0, 10), rate = 1)
```

---

ppp_sequential	<i>Simulate a homogeneous Poisson Point Process over (t_min, t_max]</i>
----------------	---

---

**Description**

Simulate a homogeneous Poisson Point Process over (t\_min, t\_max]

**Usage**

```
ppp_sequential(
  range_t = c(0, 10),
  rate = 1,
  tol = 10^-6,
  rng_stream = NULL,
  atmost1 = FALSE
)
```

**Arguments**

range_t	(vector, double) min and max of the time interval
rate	(scalar, double) constant instantaneous rate
tol	the probability that we will have more than the drawn events in (t_min, t_max]
rng_stream	an rstream object
atmost1	boolean, draw at most 1 event time

**Value**

a vector of event times t if no events realize, it will have 0 length

**Examples**

```
x <- ppp_sequential(range_t = c(0, 10), rate = 1, tol = 10^-6)
```

---

read_code	<i>Read code from text file as string</i>
-----------	---

---

**Description**

Read code from text file as string

**Usage**

```
read_code(codeFile)
```

**Arguments**

codeFile	Path to file
----------	--------------

**Value**

codeFile contents as a character string

---

rng_stream_rexp	<i>Exponential random samples from rstream objects</i>
-----------------	--

---

**Description**

Sample from rstream objects

**Usage**

```
rng_stream_rexp(size = 1, rate = 1, rng_stream = NULL)
```

**Arguments**

size	Integer, number of samples
rate	Positive number, the rate (i.e., 1/mean)
rng_stream	(rstream) an rstream object or NULL

**Value**

a vector of exponential variates of size size

**Examples**

```
rng_stream_rexp(10)
```

---

rng_stream_rpois	<i>Poisson random samples from rstream objects</i>
------------------	--

---

**Description**

Sample from rstream objects

**Usage**

```
rng_stream_rpois(size = 1, lambda = 1, rng_stream = NULL)
```

**Arguments**

size	Integer, number of samples
lambda	Positive number, the mean
rng_stream	(rstream) an rstream object or NULL

**Value**

a vector of counts of size size

**Examples**

```
rng_stream_rpois(10)
```

---

rng_stream_runif	<i>Uniform random samples from rstream objects</i>
------------------	--

---

**Description**

Sample from rstream objects

**Usage**

```
rng_stream_runif(size = 1, minimum = 0, maximum = 1, rng_stream = NULL)
```

**Arguments**

size	Integer, number of samples
minimum	Lower bound
maximum	Upper bound
rng_stream	(rstream) an rstream object or NULL

**Value**

a vector of uniform variates of size size

**Examples**

```
rng_stream_runif(10)
```

---

rng_stream_rztpois	<i>Zero-truncated Poisson random samples from rstream objects</i>
--------------------	---

---

**Description**

Sample from rstream objects

**Usage**

```
rng_stream_rztpois(size = 1, lambda = 1, rng_stream = NULL)
```

**Arguments**

size	Integer, number of samples
lambda	Positive number, the mean of the original (untruncated) Poisson distribution
rng_stream	(rstream) an rstream object or NULL

**Value**

a vector of non zero counts of size size

**Examples**

```
rng_stream_rztpois(10)
```

---

rztpois	<i>Zero-truncated Poisson random samples (basic R)</i>
---------	--

---

**Description**

Sample zero-truncated Poisson random samples (basic R)

**Usage**

```
rztpois(size = 1, lambda = 1)
```

**Arguments**

size	Integer, number of samples
lambda	Positive number, the mean of the original (untruncated) Poisson distribution

**Value**

a vector of non zero counts of size size

**Examples**

```
rztpois(10, 1)
rztpois(10, 1:10)
```

---

simpson_num_integr	<i>Simpson's method to integrate a univariate function.</i>
--------------------	---

---

**Description**

Simpson's method to integrate a univariate continuous function. Faster than R's `integrate()` and precise enough, but does not do any checks. The error is at most  $M (b-a)^5 / (180 n^4)$  where  $M$  is the maximum of the fourth derivative of the integrand in the interval  $[a, b]$ .

**Usage**

```
simpson_num_integr(f, a, b, n)
```

**Arguments**

f	function that takes a single argument
a	the lower limit of integration
b	the upper limit of integration
n	integer, number of integration points with a and b

**Value**

numeric, the integration value examples #expect 1 simpson\_num\_integr(sin, 0, pi/2, 100) #max error for simpson\_num\_integr(sin, 0, pi/2, 100) is  $5.312842e-10 \frac{1}{1} * (\pi/2 - 0)^5 / (180 * 100^4)$

---

vdraw	<i>Vectorized generic function for simulating from NHPPPs given the intensity function or the cumulative intensity function</i>
-------	---

---

**Description**

This is a wrapper to the package's specific functions, and thus slightly slower. For time-intensive simulations prefer one of the specific functions.

**Usage**

```
vdraw(
  lambda = NULL,
  lambda_args = NULL,
  Lambda_maj_matrix = NULL,
  lambda_maj_matrix = NULL,
  range_t = NULL,
  tol = 10^-6,
  atmost1 = FALSE,
  atleast1 = FALSE,
  use_cpp = FALSE
)
```

**Arguments**

lambda	(function) a vectorized intensity function, with one or two arguments. The first is time. The optional second (should be named lambda_args) is a named list with additional arguments.
lambda_args	(list) optional list of named arguments for lambda()
Lambda_maj_matrix	(matrix) for the majorizeintegrated intensity rates at the end of each interval
lambda_maj_matrix	(matrix) intensity rates, one per interval
range_t	(vector, or matrix) t_min and t_max, possibly vectorized

tol	(scalar, double) tolerance for the number of events
atmost1	boolean, draw at most 1 event time
atleast1	boolean, draw at least 1 event time in interval
use_cpp	boolean, use C++ code

**Value**

a vector of event times

**Examples**

```
Z <- vdraw(
  lambda = function(x, lambda_args = NULL) 0.1 * x,
  range_t = c(1, 10),
  lambda_maj_matrix = matrix(rep(1, 5), nrow = 1),
  atmost1 = FALSE, atleast1 = FALSE, use_cpp = TRUE
)
```

---

vdraw\_intensity\_step\_regular

*Vectorized sampling from a non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant majorizers (C++)*

---

**Description**

Vectorized sampling from a non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant majorizers. The majorizers are step functions over equal-length time intervals.

**Usage**

```
vdraw_intensity_step_regular(
  lambda = NULL,
  lambda_args = NULL,
  Lambda_maj_matrix = NULL,
  lambda_maj_matrix = NULL,
  range_t = NULL,
  subinterval = NULL,
  tol = 10^-6,
  atmost1 = FALSE,
  atmostB = NULL
)
```

**Arguments**

lambda	(function) a vectorized intensity function, with one or two arguments. The first is time. The optional second is a named list with additional arguments.
lambda_args	(list) optional list of named arguments for lambda()
Lambda_maj_matrix	(matrix) for the majorizeintegrated intensity rates at the end of each interval
lambda_maj_matrix	(matrix) intensity rates, one per interval
range_t	(vector, or matrix) t_min and t_max, possibly vectorized
subinterval	(matrix, double) subinterval of range_t to sample from
tol	(scalar, double) tolerance for the number of events
atmost1	boolean, draw at most 1 event time
atmostB	If not NULL, draw at most B (B>0) event times. NULL means ignore.

**Value**

a matrix of event times (columns) per draw (rows) NAs are structural empty spots

**Examples**

```
Z <- vdraw_intensity_step_regular(
  lambda = function(x, lambda_args = NULL) 0.1 * x,
  range_t = c(1, 10),
  lambda_maj_matrix = matrix(rep(1, 5), nrow = 1)
)
```

---

vdraw\_intensity\_step\_regular\_cpp

*Vectorized sampling from a non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant majorizers (C++)*

---

**Description**

Vectorized sampling from a non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant majorizers. The majorizers are step functions over equal-length time intervals.

**Usage**

```
vdraw_intensity_step_regular_cpp(
  lambda = NULL,
  lambda_args = NULL,
  Lambda_maj_matrix = NULL,
  lambda_maj_matrix = NULL,
```

```

range_t = NULL,
subinterval = NULL,
tol = 10^-6,
atmost1 = FALSE,
atmostB = NULL
)

```

### Arguments

**lambda** (function) a vectorized intensity function, with one or two arguments. The first is time. The optional second is a named list with additional arguments.

**lambda\_args** (list) optional list of named arguments for lambda()

**Lambda\_maj\_matrix** (matrix) for the majorizeintegrated intensity rates at the end of each interval

**lambda\_maj\_matrix** (matrix) intensity rates, one per interval

**range\_t** (vector, or matrix) t\_min and t\_max, possibly vectorized

**subinterval** (matrix, double) subinterval of range\_t to sample from

**tol** (scalar, double) tolerance for the number of events

**atmost1** boolean, draw at most 1 event time

**atmostB** If not NULL, draw at most B (B>0) event times. NULL means ignore.

### Value

a matrix of event times (columns) per draw (rows) NAs are structural empty spots

### Examples

```

Z <- vdraw_intensity_step_regular_cpp(
  lambda = function(x, lambda_args = NULL) 0.1 * x,
  range_t = c(1, 10),
  lambda_maj_matrix = matrix(rep(1, 5), nrow = 1)
)

```

---

vdraw\_intensity\_step\_regular\_R

*Vectorized sampling from a non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant majorizers (R)*

---

### Description

Vectorized sampling from a non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant majorizers. The majorizers are step functions over equal-length time intervals.

**Usage**

```
vdraw_intensity_step_regular_R(
  lambda = NULL,
  lambda_args = NULL,
  Lambda_maj_matrix = NULL,
  lambda_maj_matrix = NULL,
  range_t = NULL,
  tol = 10^-6,
  atmost1 = FALSE,
  force_zt_majorizer = FALSE,
  ...
)
```

**Arguments**

<code>lambda</code>	(function) a vectorized intensity function, with one or two arguments. The first is time. The optional second is a named list with additional arguments.
<code>lambda_args</code>	(list) optional list of named arguments for <code>lambda()</code>
<code>Lambda_maj_matrix</code>	(matrix) for the majorizeintegrated intensity rates at the end of each interval
<code>lambda_maj_matrix</code>	(matrix) intensity rates, one per interval
<code>range_t</code>	(vector, or matrix) <code>t_min</code> and <code>t_max</code> , possibly vectorized
<code>tol</code>	(scalar, double) tolerance for the number of events
<code>atmost1</code>	boolean, draw at most 1 event time
<code>force_zt_majorizer</code>	boolean, force the use of the zero-truncated majorizer; - used for flexibility in calling from other functions. Keep the default FALSE unless you know what you are doing.
<code>...</code>	(any) other arguments (ignored – used for flexibility in calling from other functions)

**Value**

a matrix of event times (columns) per draw (rows) NAs are structural empty spots

**Examples**

```
Z <- vdraw_intensity_step_regular_R(
  lambda = function(x, lambda_args = NULL) 0.1 * x,
  range_t = c(1, 10),
  lambda_maj_matrix = matrix(rep(1, 5), nrow = 1)
)
```

---

vdraw\_sc\_step\_regular *Vectorized sampling from NHPPs with piecewise constant intensities with same interval lengths (R)*

---

### Description

Simulate a piecewise constant-rate Poisson Point Process over  $(t_{\min}, t_{\max}]$  (inversion method) where the intervals have the same length (are "regular").

### Usage

```
vdraw_sc_step_regular(
  Lambda_matrix = NULL,
  lambda_matrix = NULL,
  range_t = c(0, 10),
  tol = 10^-6,
  atmost1 = FALSE,
  atleast1 = FALSE,
  use_cpp = TRUE
)
```

### Arguments

Lambda_matrix	(matrix) integrated intensity rates at the end of each interval
lambda_matrix	(matrix) intensity rates, one per interval
range_t	(vector, double) $t_{\min}$ and $t_{\max}$
tol	(scalar, double) tolerance for the number of events
atmost1	boolean, draw at most 1 event time
atleast1	boolean, draw at least 1 event time (zero-truncated NHPPP)
use_cpp	(boolean, TRUE) use the C++ implementation of the function

### Value

a vector of event times  $t$  if no events realize, it will have 0 length

### Examples

```
x <- vdraw_sc_step_regular(Lambda_matrix = matrix(1:5, nrow = 1))
```

---

vdraw\_sc\_step\_regular\_cpp

*Vectorized sampling from NHPPs with piecewise constant intensities  
with same interval lengths (C++)*

---

### Description

Simulate a piecewise constant-rate Poisson Point Process over  $(t_{\min}, t_{\max}]$  (inversion method) where the intervals have the same length (are "regular").

### Usage

```
vdraw_sc_step_regular_cpp(
  lambda_matrix = NULL,
  Lambda_matrix = NULL,
  range_t = NULL,
  subinterval = NULL,
  tol = 10^-6,
  atmost1 = FALSE,
  atmostB = NULL
)
```

### Arguments

`lambda_matrix` (matrix) intensity rates, one per interval

`Lambda_matrix` (matrix) integrated intensity rates at the end of each interval

`range_t` (vector, double)  $t_{\min}$  and  $t_{\max}$

`subinterval` (matrix, double) subinterval of `range_t` to sample from

`tol` (scalar, double) tolerance for the number of events

`atmost1` boolean, draw at most 1 event time

`atmostB` If not NULL, draw at most B ( $B > 0$ ) event times. NULL means ignore.

### Value

a vector of event times  $t$  if no events realize, it will have 0 length

### Examples

```
x <- vdraw_sc_step_regular(Lambda_matrix = matrix(1:5, nrow = 1))
```

---

 vdraw\_sc\_step\_regular\_R

*Vectorized sampling from NHPPs with piecewise constant intensities with same interval lengths (R)*

---

### Description

Simulate a piecewise constant-rate Poisson Point Process over  $(t_{\min}, t_{\max}]$  (inversion method) where the intervals have the same length (are "regular").

### Usage

```
vdraw_sc_step_regular_R(
  Lambda_matrix = NULL,
  lambda_matrix = NULL,
  range_t = c(0, 10),
  tol = 10^-6,
  atmost1 = FALSE
)
```

### Arguments

`Lambda_matrix` (matrix) integrated intensity rates at the end of each interval  
`lambda_matrix` (matrix) intensity rates, one per interval  
`range_t` (vector, double)  $t_{\min}$  and  $t_{\max}$   
`tol` (scalar, double) tolerance for the number of events  
`atmost1` boolean, draw at most 1 event time

### Value

a vector of event times  $t$  if no events realize, it will have 0 length

### Examples

```
x <- vdraw_sc_step_regular_R(Lambda_matrix = matrix(1:5, nrow = 1))
```

---

 vztdraw\_intensity\_step\_regular

*Vectorized sampling from a zero-truncated non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant\_majorizers*

---

### Description

Vectorized sampling from a zero-truncated non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant\_majorizers. The majorizers are step functions over equal-length time intervals.

### Usage

```
vztdraw_intensity_step_regular(
  lambda = NULL,
  lambda_args = NULL,
  Lambda_maj_matrix = NULL,
  lambda_maj_matrix = NULL,
  range_t = NULL,
  tol = 10^-6,
  atmost1 = FALSE,
  ...
)
```

### Arguments

lambda	(function) a vectorized intensity function, with one or two arguments. The first is time. The optional second is a named list with additional arguments.
lambda_args	(list) optional list of named arguments for lambda()
Lambda_maj_matrix	(matrix) for the majorizeintegrated intensity rates at the end of each interval
lambda_maj_matrix	(matrix) intensity rates, one per interval
range_t	(vector, or matrix) t_min and t_max, possibly vectorized
tol	(scalar, double) tolerance for the number of events
atmost1	boolean, draw at most 1 event time
...	(any) other arguments (ignored – used for flexibility in calling from other functions)

### Value

a matrix of event times (columns) per draw (rows) NAs are structural empty spots

**Examples**

```
Z <- vztdraw_intensity_step_regular(
  lambda = function(x, lambda_args = NULL) 0.1 * x,
  range_t = c(1, 10),
  lambda_maj_matrix = matrix(rep(1, 5), nrow = 1)
)
```

---

```
vztdraw_intensity_step_regular_R
```

*Vectorized sampling from a zero-truncated non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant\_majorizers (R)*

---

**Description**

Vectorized sampling from a zero-truncated non homogeneous Poisson Point Process (NHPPP) from an interval (thinning method) with piecewise constant\_majorizers. The majorizers are step functions over equal-length time intervals.

**Usage**

```
vztdraw_intensity_step_regular_R(
  lambda = NULL,
  lambda_args = NULL,
  Lambda_maj_matrix = NULL,
  lambda_maj_matrix = NULL,
  range_t = NULL,
  tol = 10^-6,
  atmost1 = FALSE,
  ...
)
```

**Arguments**

lambda	(function) a vectorized intensity function, with one or two arguments. The first is time. The optional second is a named list with additional arguments.
lambda_args	(list) optional list of named arguments for lambda()
Lambda_maj_matrix	(matrix) for the majorizeintegrated intensity rates at the end of each interval
lambda_maj_matrix	(matrix) intensity rates, one per interval
range_t	(vector, or matrix) t_min and t_max, possibly vectorized
tol	(scalar, double) tolerance for the number of events
atmost1	boolean, draw at most 1 event time
...	(any) other arguments (ignored – used for flexibility in calling from other functions)

**Value**

a matrix of event times (columns) per draw (rows) NAs are structural empty spots

**Examples**

```
Z <- vztdraw_intensity_step_regular_R(
  lambda = function(x, lambda_args = NULL) 0.1 * x,
  range_t = c(1, 10),
  lambda_maj_matrix = matrix(rep(1, 5), nrow = 1)
)
```

---

vztdraw\_sc\_step\_regular

*Vectorized sampling from zero-truncated NHPPs with piecewise constant intensities with same interval lengths*

---

**Description**

Simulate a piecewise constant-rate Poisson Point Process over  $(t_{\min}, t_{\max}]$  (inversion method) where the intervals have the same length (are "regular").

**Usage**

```
vztdraw_sc_step_regular(
  Lambda_matrix = NULL,
  lambda_matrix = NULL,
  range_t = c(0, 10),
  subinterval = NULL,
  atmost1 = FALSE,
  ...
)
```

**Arguments**

<code>Lambda_matrix</code>	(matrix) integrated intensity rates at the end of each interval
<code>lambda_matrix</code>	(matrix) intensity rates, one per interval
<code>range_t</code>	(vector, double) $t_{\min}$ and $t_{\max}$
<code>subinterval</code>	(vector, double) optional – the subinterval of <code>range_t</code> to sample. If NULL, the whole <code>range_t</code> is used.
<code>atmost1</code>	boolean, draw at most 1 event time
<code>...</code>	(any) other arguments (ignored – used for flexibility in calling from other functions)

**Value**

a vector of event times  $t$  if no events realize, it will have 0 length

**Examples**

```
x <- vztdraw_sc_step_regular(Lambda_matrix = matrix(1:5, nrow = 1))
```

---

```
vztdraw_sc_step_regular_cpp
```

*Vectorized sampling from zero-truncated NHPPs with piecewise constant intensities with same interval lengths (C++)*

---

**Description**

Simulate a piecewise constant-rate Poisson Point Process over  $(t_{\min}, t_{\max}]$  (inversion method) where the intervals have the same length (are "regular").

**Usage**

```
vztdraw_sc_step_regular_cpp(
  Lambda_matrix = NULL,
  lambda_matrix = NULL,
  range_t = c(0, 10),
  subinterval = NULL,
  atmost1 = FALSE
)
```

**Arguments**

<code>Lambda_matrix</code>	(matrix) integrated intensity rates at the end of each interval
<code>lambda_matrix</code>	(matrix) intensity rates, one per interval
<code>range_t</code>	(vector, double) $t_{\min}$ and $t_{\max}$
<code>subinterval</code>	(vector, double) optional – the subinterval of <code>range_t</code> to sample. If NULL, the whole <code>range_t</code> is used.
<code>atmost1</code>	boolean, draw at most 1 event time

**Value**

a vector of event times  $t$  if no events realize, it will have 0 length

**Examples**

```
x <- vztdraw_sc_step_regular_cpp(Lambda_matrix = matrix(1:5, nrow = 1))
```

---

vztdraw\_sc\_step\_regular\_R

*Vectorized sampling from zero-truncated NHPPs with piecewise constant intensities with same interval lengths (R)*

---

## Description

Simulate a piecewise constant-rate Poisson Point Process over  $(t_{\min}, t_{\max}]$  (inversion method) where the intervals have the same length (are "regular").

## Usage

```
vztdraw_sc_step_regular_R(
  Lambda_matrix = NULL,
  lambda_matrix = NULL,
  range_t = c(0, 10),
  atmost1 = FALSE,
  ...
)
```

## Arguments

`Lambda_matrix` (matrix) integrated intensity rates at the end of each interval

`lambda_matrix` (matrix) intensity rates, one per interval

`range_t` (vector, double)  $t_{\min}$  and  $t_{\max}$

`atmost1` boolean, draw at most 1 event time

`...` (any) other arguments (ignored – used for flexibility in calling from other functions)

## Value

a vector of event times  $t$  if no events realize, it will have 0 length

## Examples

```
x <- vztdraw_sc_step_regular_R(Lambda_matrix = matrix(1:5, nrow = 1))
```

---

ztdraw\_cumulative\_intensity

*Simulate from a zero-truncated non homogeneous Poisson Point Process (zt-NHPPP) from (t\_min, t\_max) (order statistics method)*

---

## Description

Sample zero-truncated NHPPP times using the order statistics method, optionally using an rstream generator

## Usage

```
ztdraw_cumulative_intensity(
  Lambda,
  Lambda_inv = NULL,
  range_t = c(0, 10),
  range_L = c(Lambda(range_t[1]), Lambda(range_t[2])),
  rng_stream = NULL,
  atmost1 = FALSE
)
```

## Arguments

Lambda	(function, double vector) a continuous increasing R to R map which is the integrated rate of the NHPPP
Lambda_inv	(function, double vector) the inverse of Lambda()
range_t	(vector, double) min and max of the time interval
range_L	(vector, double) min and max of the transformed time interval
rng_stream	(rstream) an rstream object or NULL.
atmost1	(boolean) draw at most 1 event time

## Value

a vector of at least 1 event times

## Examples

```
x <- ztdraw_cumulative_intensity(Lambda = function(t) t + cos(t) - 1)
```

---

ztdraw_intensity	<i>Simulate size samples from a zero-truncated non homogeneous Poisson Point Process (zt-NHPPP) from (t0, t_max) (thinning method)</i>
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---

### Description

Sample zero-truncated NHPPP intensity times using the thinning method, optionally using an `rstream` generator

### Usage

```
ztdraw_intensity(
  lambda,
  lambda_maj = NULL,
  exp_maj = FALSE,
  range_t = c(0, 10),
  rng_stream = NULL,
  atmost1 = FALSE
)
```

### Arguments

<code>lambda</code>	(function) the instantaneous rate of the NHPPP. A continuous function of time.
<code>lambda_maj</code>	(double, vector) the intercept and optional slope of the majorizing linear (if <code>exp_maj = FALSE</code> ) or log-linear (if <code>exp_maj = TRUE</code> ) function in <code>range_t</code> .
<code>exp_maj</code>	(boolean) if TRUE the majorizer is $\exp(\alpha + \beta * t)$
<code>range_t</code>	(vector, double) min and max of the time interval.
<code>rng_stream</code>	( <code>rstream</code> ) an <code>rstream</code> object or NULL
<code>atmost1</code>	(boolean) draw at most 1 event time

### Value

a vector of at least 1 event times

### Examples

```
x <- ztdraw_intensity(lambda = function(t) 1 + sin(t))
```

---

`ztdraw_intensity_step` *Simulate from a zero-truncated non homogeneous Poisson Point Process (NHPPP) from  $(t_0, t_{max})$  (thinning method) with piecewise constant majorizer*

---

### Description

Sample zero-truncated NHPPP times using the thinning method, optionally using an `rstream` generator

### Usage

```
ztdraw_intensity_step(
  lambda,
  lambda_maj_vector = lambda(1:10),
  times_vector = 0:10,
  rng_stream = NULL,
  atmost1 = FALSE
)
```

### Arguments

<code>lambda</code>	(function) the instantaneous rate of the NHPPP. A continuous function of time.
<code>lambda_maj_vector</code>	(scalar, double) $K$ constant majorizing rates, one per interval
<code>times_vector</code>	(vector, double) $K+1$ time points defining $K$ intervals of constant rates: $[t_{-1} = \text{range}_t[1], t_{-2})$ : the first interval $[t_k, t_{\{k+1\})$ : the $k$ -th interval $[t_{\{K\}}, t_{\{K+1\}} = \text{range}_t[2])$ : the $K$ -th (last) interval
<code>rng_stream</code>	( <code>rstream</code> ) an <code>rstream</code> object or <code>NULL</code>
<code>atmost1</code>	boolean, draw at most 1 event time

### Value

a vector of event times (`t_`) with at least one element

### Examples

```
x <- ztdraw_intensity_step(lambda = function(t) exp(.02 * t))
```

---

ztdraw_sc_linear	<i>Simulate size samples from a zero-truncated non homogeneous Poisson Point Process (zt-NHPPP) from (t_min, t_max) with linear intensity function</i>
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---

### Description

Sample zero-truncated NHPPP times from a linear intensity function using the inversion method, optionally using an `rstream` generator

### Usage

```
ztdraw_sc_linear(  
  alpha = 1,  
  beta = 0,  
  range_t = c(0, 10),  
  rng_stream = NULL,  
  atmost1 = FALSE  
)
```

### Arguments

<code>alpha</code>	(double) the intercept
<code>beta</code>	(double) the slope
<code>range_t</code>	(vector, double) min and max of the time interval
<code>rng_stream</code>	(rstream) an rstream object
<code>atmost1</code>	(boolean) draw 1 event time

### Value

a vector of at least 1 event times

### Examples

```
x <- ztdraw_sc_linear(alpha = 0, beta = 0.2)
```

---

ztdraw_sc_loglinear	<i>Simulate from a zero-truncated non homogeneous Poisson Point Process (zt-NHPPP) from (t_min, t_max) with a log-linear intensity function (inversion method)</i>
---------------------	--

---

### Description

Sample zt-NHPPP times from an log-linear intensity function using the inversion method, optionally using an rstream generator

### Usage

```
ztdraw_sc_loglinear(
  alpha = 1,
  beta = 0,
  range_t = c(0, 10),
  rng_stream = NULL,
  atmost1 = FALSE
)
```

### Arguments

alpha	(double) the intercept in the exponent
beta	(double) the slope in the exponent
range_t	(vector, double) min and max of the time interval
rng_stream	(rstream) an rstream object.
atmost1	boolean, 1 event time

### Value

a vector of at least 1 event times

### Examples

```
x <- ztdraw_sc_loglinear(alpha = 0, beta = 0.2)
```

---

ztppp	<i>Simulate a zero-truncated homogeneous Poisson Point Process over <math>(t_{\min}, t_{\max}]</math></i>
-------	---

---

**Description**

Simulate a zero-truncated homogeneous Poisson Point Process over  $(t_{\min}, t_{\max}]$

**Usage**

```
ztppp(range_t = c(0, 10), rate = 1, rng_stream = NULL, atmost1 = FALSE)
```

**Arguments**

range_t	(vector, double) min and max of the time interval
rate	(scalar, double) constant instantaneous rate
rng_stream	an rstream object
atmost1	boolean, draw at most 1 event time

**Value**

a vector of event times of size size

**Examples**

```
x <- ztppp(range_t = c(0, 10), rate = 0.001)
```

# Index

check\_ppp\_sample\_validity, [3](#)  
check\_ppp\_vector\_validity, [4](#)  
compare\_ppp\_vectors, [4](#)  
  
draw, [5](#)  
draw\_cumulative\_intensity\_inversion, [6](#)  
draw\_cumulative\_intensity\_orderstats,  
[7](#)  
draw\_intensity, [8](#)  
draw\_intensity\_step, [9](#)  
draw\_sc\_linear, [10](#)  
draw\_sc\_loglinear, [11](#)  
draw\_sc\_step, [12](#)  
draw\_sc\_step\_regular, [13](#)  
  
expect\_no\_error, [14](#)  
  
get\_step\_majorizer, [14](#)  
  
inverse\_with\_uniroot, [15](#)  
inverse\_with\_uniroot\_sorted, [16](#)  
  
Lambda\_exp\_form, [17](#)  
Lambda\_inv\_exp\_form, [17](#)  
Lambda\_inv\_linear\_form, [18](#)  
Lambda\_linear\_form, [18](#)  
  
make\_cumulative\_Lambda\_matrix, [19](#)  
make\_lambda\_matrix, [19](#)  
make\_range\_t\_matrix, [20](#)  
mat\_cumsum\_columns, [20](#)  
mat\_cumsum\_columns\_with\_scalar\_ceiling,  
[21](#)  
mat\_cumsum\_columns\_with\_vector\_ceiling,  
[21](#)  
mat\_diff\_columns, [22](#)  
  
ppp\_n, [22](#)  
ppp\_next\_n, [23](#)  
ppp\_orderstat, [24](#)  
ppp\_sequential, [24](#)  
  
read\_code, [25](#)  
rng\_stream\_rexp, [26](#)  
rng\_stream\_rpois, [26](#)  
rng\_stream\_runif, [27](#)  
rng\_stream\_rztpois, [27](#)  
rztpois, [28](#)  
  
simpson\_num\_integr, [28](#)  
  
vdraw, [29](#)  
vdraw\_intensity\_step\_regular, [30](#)  
vdraw\_intensity\_step\_regular\_cpp, [31](#)  
vdraw\_intensity\_step\_regular\_R, [32](#)  
vdraw\_sc\_step\_regular, [34](#)  
vdraw\_sc\_step\_regular\_cpp, [35](#)  
vdraw\_sc\_step\_regular\_R, [36](#)  
vztdraw\_intensity\_step\_regular, [37](#)  
vztdraw\_intensity\_step\_regular\_R, [38](#)  
vztdraw\_sc\_step\_regular, [39](#)  
vztdraw\_sc\_step\_regular\_cpp, [40](#)  
vztdraw\_sc\_step\_regular\_R, [41](#)  
  
ztdraw\_cumulative\_intensity, [42](#)  
ztdraw\_intensity, [43](#)  
ztdraw\_intensity\_step, [44](#)  
ztdraw\_sc\_linear, [45](#)  
ztdraw\_sc\_loglinear, [46](#)  
ztppp, [47](#)